

Calculation methods for column shoe connections

TR 068 September 2018

EUROPEAN ORGANISATION FOR TECHNICAL ASSESSMENT WWW.EOTA.EU EOTA Technical Reports are developed as supporting reference documents to EOTA publications such as European Technical Approval Guidelines (ETAG) and European Assessment Documents (EAD), or other harmonised technical specifications. They can be used for technical assessments of construction products, notably when conducted by Technical Assessment Bodies (TAB) designated by European Members States in accordance to Regulation (EU) No. 305/2011 for issuing European Technical Assessments (ETA).

EOTA Technical Reports detail aspects relevant for construction products such as design, execution and evaluation of tests, and express the common understanding of existing knowledge and experience of the Technical Assessment Bodies in EOTA at a particular point in time. They may give recommendations for product packaging, transport, storage, maintenance, replacement and repair.

Where knowledge and experience is developing, especially through assessment work, such reports can be amended. Amendments of EOTA Technical Reports supersede the previous one. The reference title and language for this TR is English. The applicable rules of copyright refer to the document elaborated in and published by EOTA.

This EOTA Technical Report has been elaborated by EOTA WG 20 - Structural Metallic Products and Ancillaries; convened by VTT and has been adopted by the EOTA Technical Board.

Contents

1		Scope of the TR	4
2		Specific terms/symbols used in this TR	5
	2.1	List of Symbols	6
3		Design of column shoes and coluMn shoe connections in normal temperature	8
	3.1	General	8
	3.2 3.2 3.2	Design rules for mechanical resistance and bending stiffness of connection .1 Position of column shoes and design of connected structures	8 8 9
	3.3 3.3	Mechanical resistance of column shoes in Stage II .1 General	10 10
	3.3 3.3 3.3	 Design criterion for grouted section subjected to axial force and bending Resistance of column end Interaction of axial force, bending moment and shear force 	11 11 12
	3.4	Resistance of column shoe components and welds	14
4		Fire resistance of column shoes without cover	15
	4.1	Temperature analysis	15
	4.2	Fire rating based on temperature analysis	16
5		Analysis report	17
6		Reference documents	18

1 SCOPE OF THE TR

This Technical Report (TR) covers the structural requirements and design rules for column shoe connections with column shoes in three stages: column shoe as delivered, column shoe connection before grouting and column shoe connection in use after grouting.

This Technical Report (TR) can be used as criteria for assessing the performance and as design rules for column connections with column shoes.

This TR does not purport to address all of the safety concerns associated with its use. It is the responsibility of the user of this technical report to establish appropriate safety practices and determine the applicability of regulatory limitations prior to use.

2 SPECIFIC TERMS/SYMBOLS USED IN THIS TR

See Figure 1 for the illustration of the specific terms.



Fig. 1. Illustration of specific terms.

- *Base plate* Thick, horizontal steel plate provided with a vertical hole; fixed to a threaded anchor bolt by two nuts and two washers
- Side plate Vertical, bent or straight steel plate(s) welded to the bottom plate
- Anchor bar Vertical reinforcing bar welded to side plate
- *Rear bar* Partly vertical reinforcing bar, lower end bent, welded to side plate
- *Top plate* A thin, non-structural steel plate parallel to the base plate but above it, serves as a mould when the column is concreted

2.1 List of Symbols

A _{anc,i} A _{bolt}	nominal cross-sectional area of anchor bar <i>i</i> tensile stress area of anchor bolt				
A _{plate.i}	, nominal cross-sectional area of side plate <i>i</i>				
F _{w,I} L _{eff}	the nominal resistance of the weld joint i effective length to be used instead of l_0 when designing the column with column shoes in				
	accordance with EN 1992-1-1 :2004				
L _{lap}	lap length				
M_{Ed}	design value of bending moment (action effect)				
M_t	theoretical yielding moment of column shoe connection				
N _{anc}	sum of nominal axial resistances of straight anchor bars				
N _{anc,we} N _{bolt,nc}	sum of calculated nominal resistances of welds between straight anchor bars and side plate(s) in the direction of anchor bolt nominal axial resistance of anchor bolt				
N _{side,w}	sum of calculated nominal resistances of welds between the side plate(s) and base plate in the direction of the anchor bolt				
$N_{\scriptscriptstyle Ed}$	design value of axial load on connection				
N_{Ed}^1	design value of axial load on a single bolt or column shoe				
N _{plate}	sum of nominal axial resistances of side plates				
$N_{\scriptscriptstyle Rd}$	design value of axial resistance of column shoe and corresponding anchor bolt				
Р	point load				
V	shear force				
V_{Ed}	design value of shear load on a connection				
V_{Ed}^1	design value of shear load on a single bolt or column shoe				
V_{Pd}	design value of shear resistance of a column shoe				
ab	coefficient calculated as in EN 1993-1-8, table 3.4				
d _b	diameter of nominal stress area in thread of anchor bolt				
f _{anc,y,i}	yield strength of anchor bar <i>i</i>				
f _{base,u}	ultimate strength of base plate				
f _{bolt,u}	ultimate strength of anchor bolt				
f _{bolt,y}	yield strength of anchor bolt				
f _{plate,y,i}	nominal yield strength of side plate <i>i</i>				
f _{bolt,yd}	design yield strength of anchor bolt, used for design of column shoe connection				
h _{nut}	thickness of nut below base plate				
k 1	coefficient calculated as in EN 1993-1-8, table 3.4				
<i>k</i> L	experimental factor:				
	- if $k_L \leq 1,10$, $k_L l_0$ gives the effective length to be used instead of l_0 when designing the				

columns in accordance with EN 1992-1-1

- if kL > 1,10, the connection is assumed to be hinged in design and effective length l_0 specified in EN 1992-1-1 is used as such
- *I*₀ Euler's buckling length (effective length in EN 1992-1-1)
- *m* number of straight anchor bars or number of measured subzones outside column shoe zone
- *n* number of active column shoes, number of tests, number of subzones *Z_i* in column shoe zone
- *t*^{*r*} equivalent span of anchor bolt
- *t*grout thickness of grout
- thickness of base plate
- α_b coefficient calculated from $f_{bolt,y}$
- _{7/M2} safety factor for ultimate strength of anchor bolt, used for design of anchor bolt
- *ybolt* safety factor for yield strength of anchor bolt, used for design of column shoe
- η_d experimental stiffness factor $\leq \eta_{d,0}$
- $\eta_{d,0}$ stiffness factor \leq 1,00 given by the producer and used for the design of the test specimens
- μ friction coefficient between base plate and grout

3 DESIGN OF COLUMN SHOES AND COLUMN SHOE CONNECTIONS IN NORMAL TEMPERATURE

3.1 General

There is no one-to-one correspondence between the mechanical resistance of a *column shoe as delivered* and the mechanical resistance of a *column shoe connection*. A connection is subjected to various action effects like axial force, shear force and bending moment in different combinations, and the stiffness of the connection also has an impact on the design of the column. It is impossible to determine the mechanical resistance or stiffness of a column shoe connection as a set of values determined according to some standards. Therefore, these properties are declared as a set of design rules for the *connection or column or works* in which the column shoes are intended to be used.

A difference is made between

- the design of the column shoe as delivered (Stage 0)
- the design of the column shoe connection before grouting (Stage I)
- the design of the column shoe connection after the grout has hardened (Stage II)
- the design of the anchor bolts

The methods used to justify both the design of the column shoes and the design rules for the column shoe connections are given. This is how the word *verification* is understood here.

The design rules for the column shoe connections are given in Section 3.2.

The design of the anchor bolts shall be carried out according to their European Technical Assessment (ETA) or Eurocodes when applicable.

Some design rules for the column shoe connections only reflect the properties of the anchor bolt. This is explained by the fact that, *in order to facilitate the design of the connection and column, the manufacturer claims, that the column shoe is strong enough to carry a certain share of the loads which the related anchor bolt is able to carry.* Consequently, the methods used to verify such design rules aim at checking whether this claim is in force.

The tensile resistance of the anchor bolt given cannot always be 100% exploited because the tension in the column shoe is eccentric with respect to the centroidal axis of the bolt and because the yielding reduces the bending stiffness of the connection in such a way that the design of slender columns requires additional considerations. This is reflected in the design rules which are based on the yield strength of the anchor bolt instead of the ultimate strength.

3.2 Design rules for mechanical resistance and bending stiffness of connection

3.2.1 Position of column shoes and design of connected structures

In ordinary cases the column shoes are placed in the corners of a column as shown in Fig. 2.a. Intermediate columns shoes, see Fig. 2.d, are used if the resistance of those in the corners is not high enough or when the tensile forces cannot be properly transferred through the corners of the concrete element only (Fig. 2.b). In some cases two columns shoes per column may be enough (Fig. 2.c).

Column shoes for which kL = 1,1 have no requirement for the rigidity and the columns with such column shoes or connections with less than four column shoes can only be designed assuming that the connection with the column shoes is hinged in Stage II.

The distance between the column shoes is determined by the transfer of the forces from the anchor bars to the concrete element and from the anchor bolt to the foundation. In all cases shall the concrete structures be designed to carry the concentrated loads due to the column shoes and anchor bolts.



Fig. 2. Examples of column shoe configurations.

3.2.2 Mechanical resistance of column shoes in Stage I

3.2.2.1 Action effects

Before grouting the connection, the normal force N_{Ed}^1 for a single column shoe is calculated from the total normal force N_{Ed} and bending moment M_{Ed} acting at the connection, assuming that the column shoes act as an infinitely stiff plate fixed rigidly to the end of the column. This is also assumed when calculating the normal force and bending moment which the anchor bolts are subjected to.

The design shear force for a column shoe is calculated by dividing the total shear force to those column shoes only which are compressed horizontally and transversely against the end of the column when the column is subjected to a shear force, see Fig. 3.



Fig. 3. Only the column shoes on the right hand side are considered active against shear.

3.2.2.2 Resistance

The resistance of a column shoe subjected to axial force and shear shall satisfy

$$\frac{16|v_{Ed}^{1}|t_{R}}{\pi d_{b}^{3}} + \frac{4|v_{Ed}^{1}|}{\pi d_{b}^{2}} \le f_{bolt,yd}$$
(1)

where, see Fig. 4,

- V_{Ed}^{1} = design value of shear load on a single bolt (action effect)
- N_{Ed}^{1} = design value of axial load on a single bolt (action effect), calculated from the total axial force N_{Ed} and bending moment M_{Ed}
- d_b = diameter of nominal stress area in thread of anchor bolt
- $t_R = t_{grout} h_{nut} + d_b/2$
- $f_{bolt,yd}$ = yield strength of bolt steel, see Eq. (3)



Fig 4. Loads and parameters characterising the column shoe connection in Stage I.

3.3 Mechanical resistance of column shoes in Stage II

3.3.1 General

When calculating the action effects of a column, the rigidity of the end connections has to be estimated. A connection of a precast column comprising anchor bolts and column shoes may be less rigid than a continuously reinforced connection between a cast-in-place column and foundation. On the other hand, the additional reinforcing bars anchoring the column shoes to the column make the anchoring zone stiffer than the rest of the column. The net effect of these two factors is taken into account by experimental factor k_L determined in initial type tests, see TR 067. The columns with column shoes at the lower end with boundary conditions illustrated in EN 1992-1-1, Fig. 5.7 cases b), c), d), and e) are designed replacing the effective length l_0 by

$$L_{\rm eff} = k_L l_0 \tag{2}$$

when k_L is $\leq 1,10$. When k_L is > 1,10, the column shoe connection is considered hinged.

For cases f) and g) in Fig. 5.7 of EN 1992-1-1, the flexibilities k_i in equations 5.15 and 5.16 of EN 1992-1-1 are replaced by $k_i k_{L^2}$ at each connection *i* provided with column shoes.

When calculating the resistance of the connection, four different cases are considered:

- 1. Resistance of the grouted connection subjected to axial load and bending
- 2. Shear resistance of individual column shoes subjected to compression
- 3. Shear resistance of individual column shoes subjected to tension
- 4. Resistance of the column end

3.3.2 Design criterion for grouted section subjected to axial force and bending

The resistance of the grouted section above the foundation and below the column shoes is calculated according to EN 1992-1-1 assuming that the section behaves as a concrete section reinforced with the anchor bolts. For the bolts, the bilinear stress-strain assumption with a horizontal top branch (EN 1992-1-1, 3.2.7 b) is applied assuming that the design strength of the anchor bolt is

 $f_{bolt,yd} = \min\{\eta_d f_{bolt,y} / \gamma_{M2}; f_{bolt,u} / \gamma_{bolt}\}$

(3)

where

η_d	=	stiffness factor \leq 1,00: the value is determined in initial type tests
f _{bolt,y}	=	yield strength of steel in the anchor bolt
f _{bolt,u}	=	the ultimate strength of steel in the anchor bolt
<i>Υ</i> Μ2	=	material safety factor according to EN 1993-1-8, Table 2.1
γbolt	=	material safety factor of anchor bolt according to the relevant European Technical
		Assessment (ETA) or Eurocodes when applicable

Note: According to EN 898-1, the resistance of the anchor bolts is controlled by $f_{bolt,u}$. However, the tensile and bending resistance of a column shoe connection has to be controlled by $f_{bolt,y}$ because, after yielding, the bending stiffness of the connection becomes indefinite, which makes reasonable structural design impossible. $f_{bolt,y}$ is always $< f_{bolt,u}$ but due to η_d and the nationally determined parameters γ_{M2} and γ_{bolt} , $\eta_d f_{bolt,y} / \gamma_{M2} > f_{bolt,u} / \gamma_{bolt}$ may also be true. For this reason, Eq. (3) includes two strength values.

3.3.3 Resistance of column end

The resistance of the column end subjected to axial load, shear and bending is calculated according to EN 1992-1-1 and EN 1993-1-8. Particularly, the main reinforcement shall be extended down to the column shoe level and the lap length, see Fig. 5, shall meet the requirements given in EN 1992-1-1, Chapter 8.7.



Fig. 5. Determining lap length L_{lap} . The fillet welds and the side plate next to the anchor bar reduce the bond effectively.

3.3.4 Interaction of axial force, bending moment and shear force

3.3.4.1 General

Interaction of axial force, bending moment and shear force is taken into account by considering each individual column shoe separately. Since the bending and axial loading result in tensile or compressive forces in the individual column shoe - anchor bolt combinations, the interaction problem is simplified to interaction of normal force and shear force.

3.3.4.2 Action effects

The action effects at the connection are first divided to the individual column shoes.

The axial force N_{Ed}^{1} for a single anchor bolt or column shoe is calculated from the total axial force N_{Ed} and bending moment M_{Ed} acting at the connection, assuming that the column shoes act as an infinitely stiff plate, fixed rigidly to the end of the column, and the grouted connection behaves as a concrete section reinforced with the anchor bolts.

The design value of the shear force for a single column shoe on the active side is calculated from

$$V_{Ed}^{I} = \frac{V_{Ed} - \mu N_{Ed}}{n} \tag{4}$$

where

 V_{Ed} = the design value of the total shear force

 N_{Ed} = the design value of the total axial compressive force

n = the number of the individual column shoes which are horizontally and transversely compressed against the end of the column due to the shear force. The column shoes at the opposite side of the connection are ignored when calculating the shear resistance, see Fig. 3.

3.3.4.3 Resistance of column shoe in axial loading

The resistance of a column shoe in tension and compression is calculated from

$$N_{Rd} = f_{bolt, yd} A_{bolt}$$

where

 $f_{bolt,yd}$ = design strength of steel in the anchor bolt, see Eq. (3)

 A_{bolt} = stress area in thread of anchor bolt

3.3.4.4 Shear resistance of column shoe

The shear resistance of a column shoe is calculated according to EN 1993-1-8, Chapter 6.2.2, from

$$V_{Rd} = k_s V_t = k_s \min\{F_{1,vb,Rd}; F_{2,vb,Rd}\}$$
(6)

where $F_{1,vb,Rd}$ and $F_{2,vb,Rd}$ are obtained from

(5)

$$F_{I,vb,Rd} = 0.8 \frac{k_I a_b f_{base,u} d_b t_{base}}{\gamma_{M2}}$$
(7)

$$F_{2,vb,Rd} = \frac{\alpha_b f_{bolt,u} A_{bolt}}{\gamma_{M2}}$$
(8)

$$\alpha_b = 0.44 - (0.0003MPa^{-1}) f_{bolt,y}$$
(9)

In these expressions

k _s	=	a parameter determined in accordance with TR 067, Chapter 6
k_1 and a_b	=	coefficients calculated as in EN 1993-1-8, Table 3.4
f _{base,u}	=	the ultimate strength of the base plate
d_b	=	diameter of nominal stress area in thread of anchor bolt
t _{base}	=	thickness of the base plate
ΎM2	=	material safety factor according to EN 1993-1-8, Table 2.1
f _{bolt,u}	=	ultimate strength of steel of the anchor bolt
Abolt	=	tensile stress area of the anchor bolt

3.3.4.5 Design criterion for column shoe subjected to shear and axial load

The shear resistance of a column shoe subjected to shear and compression shall meet the requirement

$$V_{Ed}^{I} \le V_{Rd} \tag{10}$$

where $V_{\rm Ed}^{\rm I}$ and $V_{\rm Rd}$ are calculated from Equations (4) and (6), respectively.

The simultaneous tensile force N_{Ed}^{I} and shear force V_{Ed}^{I} in each column shoe shall satisfy the conditions

$$\frac{\left|N_{Ed}^{1}\right|}{1,4N_{Rd}} + \frac{\left|V_{Ed}^{1}\right|}{V_{Rd}} \le 1$$
(11)

$$\frac{N_{Ed}^1}{N_{Rd}} \le 1 \tag{12}$$

where $\,N_{_{Rd}}\,$ and $\,V_{_{Rd}}\,$ are calculated from Equations (5) and (6), respectively.

3.4 Resistance of column shoe components and welds

As a part of the initial type testing, the axial yield resistance of the

- reinforcing bars (anchor bars)
- side plates
- welds connecting the reinforcing bars to the base plate and side plates and
- welds connecting the side plates to the base plate

are calculated according to EN 1992-1-1, EN 1993-1-1 and EN 1993-1-8, whichever is relevant. When doing so, it is assumed that the different components of the column shoe as well as their connections are subjected to axial load and the material safety coefficients are set equal to 1,0.

The sum of the calculated axial resistances of all anchor bars 1,...,m, the rear bar excluded, shall be

$$N_{anc} = \sum_{i=1}^{m} f_{anc,y,i} A_{anc,i} \ge N_{bolt,nom} = f_{bolt,y} A_{bolt}$$
(13)

where

f _{anc,y,i}	=	the nominal yield strength of anchor bar i
A _{anc,i}	=	nominal cross-sectional area of anchor bar <i>i</i>
N _{bolt,nom}	=	nominal axial resistance of anchor bolt
f _{bolt,y}	=	nominal yield strength of anchor bolt
Abolt	=	stress area in thread of anchor bolt

The sum of the calculated axial resistances of the side plates 1, ..., q,

$$N_{plate} = \sum_{i=1}^{q} f_{plate, y, i} A_{plate, i}$$
(14)

shall be able to carry the yield force from the anchor bolt which is eccentric with respect to centroid of section of side plate(s). Here

 $f_{plate,y,i}$ = the nominal strength of the steel in side plate *i* $A_{plate,i}$ = nominal cross-sectional area of the active part of anchor side plate *i*

 $N_{side, weld}$, the sum of the calculated nominal resistances of the welds 1,..., *p* between the side plates and the base plate, calculated in the direction of the anchor bolt, shall be able to carry the eccentric nominal yield force from the anchor bolt. $N_{side, weld}$ is calculated according to EN 1993-1-8, Chapter 4.5 assuming axial tension in the side plates.

$$N_{side,weld} = \sum_{i=1}^{p} F_{w,i} \tag{155}$$

where

 $F_{w,i}$ = the nominal resistance of the weld joint *i*

The sum of the calculated nominal resistances of the welds between the side plates and the anchor bars *i*, the rear bar excluded, shall be able to carry the eccentric yield force from the anchor bolt. The summation is extended over all straight bars welded to the side plate(s).

15/18

4 FIRE RESISTANCE OF COLUMN SHOES WITHOUT COVER

4.1 Temperature analysis

In the analysis, the column shoe is exposed to the standard fire according to EN 1363-1. Three-dimensional finite element analysis is applied. The temperature field of the column shoe is calculated and compared with the experimental temperatures obtained in initial tests specified in TR 067, Chapter 8. If necessary, the calculation method is modified to give a safe prediction for the temperature distribution.

The geometric model for the analysis of the connection is illustrated in Fig. 6. It is assumed that the column shoes considered connect two columns with the same square cross-section. The lower column is provided with anchor bolts and the upper one with column shoes placed along the outer faces of the columns. To simplify the calculations, it is assumed that the connection is positioned in such a way that the foundation, beams and floors can be ignored.



Fig. 6. Overview on model. The coloured zone is included in analysis. Either 1/8 (a) or1/4 (b) of the cross-section can be included in the model.

Surfaces S_1 and S_2 shown in Fig. 6 are subjected to heat transfer by convection and radiation from fire. Other surfaces of the model are assumed to be perfectly insulated.

In vertical direction, the modelled zone shall cover at least the minimum measures shown in Fig. 7.

Three-dimensional volume elements are used for steel and concrete. The circular bars and anchor bolts may be modelled with coaxial rectangular elements which have the same cross-sectional area. Chamfered steel parts and the concrete column may be modelled as if they were non-chamfered.



Fig. 7. Minimum size of the model.

The thermal conductivity, specific heat, coefficient of heat transfer by convection and surface emissivity for the concrete and steel are taken from EN 1992-1-2 and 1993-1-2, respectively. For the concrete, both the upper and lower limit of the thermal conductivity and the moisture content u = 0% are applied.

4.2 Fire rating based on temperature analysis

The fire rating for the unprotected column shoes is done based on the following principles.

In European Technical Assessment:

1. A temperature analysis is carried out for all sizes of column shoe of each family. For all analyses, the minimum possible column section is chosen. For all column shoes the temperature in the critical point of the column shoe is given in the European Technical Assessment at relevant time intervals (15 min, 20 min, 30 min, 45 min, 60 min, 90 min, 120min,...).

In Design:

- 2. When the column shoes are in compression, the fire rating for the shoe is the same as that for the column.
- When the column shoe is in tension, the fire rating is determined by the temperature and the utilisation level of the tensile resistance. The relevant design rules given in EN 1992-1-2 and EN 1993-1-2 are applied.

5 ANALYSIS REPORT

The report shall include the calculations to verify that the requirements presented in Section 3.4 for the column shoe components and welds are fulfilled. In addition, the justification of the temperature analysis method, based on fire tests performed and reported according to TR 067, as well as the fire rating process shall be documented in the report.

6 **REFERENCE DOCUMENTS**

As far as no edition date is given in the list of thereafter, the publication in its current version is of relevance.

EAD 200102-00-0302	Evaluation Assessment Document of Column Shoes
EN 1363-1	Fire resistance tests. Part 1: General Requirements
EN 1990	Eurocode - Basis of structural design
EN 1992-1-1	Eurocode 2: Design of concrete structures - Part 1-1: General rules and rules for buildings
EN 1992-1-2	Eurocode 2: Design of concrete structures - Part 1-2: General rules - Structural fire design
EN 1993-1-1	Eurocode 3: Design of steel structures - Part 1-1: General rules and rules for buildings
EN 1993-1-2	Eurocode 3: Design of steel structures - Part 1-2: General rules - Structural fire design
EN 1993-1-8	Eurocode 3: Design of steel structures - Part 1-8: Design of joints
TR 067	Bending of column shoe connections